An energy management scheme for improving the fuel economy of a fuel cell/battery/supercapacitor-based hybrid electric vehicle using the coyote optimization algorithm (COA)

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This study describes a multi-input power system that is suited for fueling electric automobiles, Intercitys, and airplanes, particularly in situations with significant fluctuating load demand. The dual framework utilizes fuel cells (FC), batteries, and super capacitors (SCs). An energy management system (EMS) remains a critical aspect of lowering overall hydrogen consumption and minimizing the degradation of FC functionality. A novel EMS that has been suggested focused on a novel optimization method known as the Coyote optimization algorithm (COA), and it considers the fact that the total load is adequately supplied within the limitations of each power source. To minimize the hydrogen consumption. By maximizing the power generated by the energy storage devices, the energy acquired from the FC is reduced. In comparison to other optimization methods, the COA would be a practical, effective, and relatively straightforward optimizer that only involves a limited number of controlling factors to be set. The framework application MATLAB/Simulink is used to create the proposed method. In order to show the effectiveness of the proposed methodology, a study with several different conventional techniques is performed, which includes the classic Proportional-Integral control mechanism, the Frequency Decoupling with State Machine (FDSM) controlling technique, the equivalent consumption minimization scheme (ECMS), and the external energy minimization scheme (EEMS). The efficacy of the algorithm and the FC's aggregate H2 usage serve as the focal points for comparison in this work. The outcomes demonstrate that the recommended COA strategy is superior and more effective than the alternative approaches.

KEYWORDS
COA, hybrid electric vehicle, hydrogen consumption, power management scheme, system efficiency electric vehicle, energy management system, system efficiency, coyote algorithm

Abbreviations: EV, Electric Vehicle; EMS, Energy Management Structure; HEVs, Hybrid Electric Vehicles; COA, Coyote Optimization algorithm; PMS, Power Management Strategy; PI, Proportional Integral; BESSs, Battery Energy Storage Systems; Li-ion, Lithium-Ion; FLC, Fuzzy Logic Controller; PMU, Power Management Unit.
1 Introduction

Nowadays, environmental protection, decrement in conventional energy storage systems, and emission-free energy storage classifications affect performance in many parts of the world. Conventional vehicles are mainly designed with internal combustion engine (ICEs) which uses fossil fuel; these vehicles release harmful emissions and high noise, and the cost of fuel is high. To solve these issues, Dr. Ferdinand Porsche developed the first electric vehicle (Egger-Lohner vehicle) in the year 1898. Electric vehicles (EVs) are divided into several categories, including battery electric vehicles (BEVs), plug-in hybrid electric cars (PHEVs), hybrid electric vehicles (HEVs), and fuel cell hybrid electric vehicles (FCEVs). These models have distinct characteristics like BEVs and have a low driving range, but the mode is emission-free and makes low noise. HEVs have both an electric and gasoline engine (ICE) and the model is not emission-free, but the driving range is high depending on energy sources. The PHEV has high efficiency when compared to BEV and HEV but this model requires an external source for charging the batteries (Banaei et al., 2020; Bauman et al., 2008; Meng et al., 2019; Galdi et al., 2006; Buccoliero et al., 2019; Li et al., 2019). The fuel cell hybrid electric vehicle was proposed to attain a higher driving range, be emission-free, and make low noise; moreover, it also overcomes the issues of the previous models, but the FHEV is a bit costly.

A power management scheme (PMS) is required to accomplish certain hybridization and meet the main purpose of spreading load requirements through power sources. The PMS considerably reduces hydrogen consumption and improves energy efficiency by limiting fuel cell performance to wider operating levels. A
traditional PMS was implemented to control the system load among various integrated input sources.

As per the American Department of Energy Studies, the proton exchange membrane fuel cell technology has been improved to 5,000 h in real-world settings with 10% less degradation; however, it is presently not over 2,500 h (Carignan et al., 2018; Khan et al., 2018; Kandidayeni et al., 2019; Wu et al., 2019; Yuan et al., 2019; Liu et al., 2020). The PEMFC is one of the types of fuel cells that help in the propulsion system for a long time. Nowadays, PEMFC has been used in many automotive HEVs because of the friendly environment, and it increases the autonomy of EVs. Sir William Grove first developed the fuel cell in 1839. Mainly, fuel cells are categorized into many types based on their characteristics. In this work, the HEV with the PEMFC has been considered because of its high energy density, lightweight, and ability to operate at low temperatures. A major part of a hybrid electric vehicle is its multiple input sources; it consists of the li-ion battery bank, ultra-capacitors/super capacitors bank, and PEMFC, utilizing different combinations because a single source alone cannot meet the requirements of the load (Khaligh et al., 2010; Penina et al., 2010; Itani et al., 2017; Pierzan and Leandro Dos, 2018; Rezk et al., 2019; Kwan et al., 2020; Lee et al., 2020; Li et al., 2020; Xiao et al., 2021).

A supercapacitor (SC) and fuel cell are used as a Hybrid energy storage system (HESS) for the HEV in (Sun et al., 2020). In (Zhang et al., 2020), the battery and fuel cell are considered an HESS in the HEV. These combinations show that it is not able to accomplish the requirement of a DC bus and HEV. Yuan et al. (2020) proposed HESS as a fuel cell/SC/battery; it is a realistic approach for attaining

![Figure 3](image1.png)  
**FIGURE 3**  
Control strategy of uni-directional converter output voltage.

![Figure 4](image2.png)  
**FIGURE 4**  
Bi-directional converter topology.
high-power density and energy, and the energy storage capacity is also more. Hybridization of fuel cells, Li-ion batteries, and SC leads to better fuel economy, and these batteries and SC provide a better part of load performance.

The HESS relates to uni-directional and bi-directional DC-DC converters for efficient exchange of power. Various configurations of converters for HEV are addressed in Rezk et al. (2021) to distribute the power of HESS to load or load to HESS through different power management strategies (PMS). In designing the proper PMS, it will achieve the optimal economy of fuel. PMS should be limited as much as possible in hybrid energy sources because it can impact the life cycle of hybrid sources.

Kamel et al. (2020) developed state machine control; it is a simple design. The design comes under a rule-based scheme based on heuristic previous experience with the PMS in each state or under the rules that were developed. Here, the performance mainly depends on the designer of the system, particularly how well it is appropriate to the operation of all the components in the system. Tao et al. (2020) implemented a rule-based fuzzy logic PMS. The power exchange was done by the membership functions, and it was also done by a set of IF-THEN rules. Here, the fuzzy controller was based on IF-THEN rules that mainly required experience and knowledge. This strategy could be tuned easily for optimal operation of the system (Yue et al., 2019; Imran et al., 2020; López-Pérez et al., 2020; Chen et al., 2019; Ouddah et al., 2019; Alam et al., 2020).

The classical PI controller was proposed by Nguyen et al. (2020). It controlled mainly the state of charge of the battery, DC Bus voltage, and UC voltage by using PI control. These control schemes could be tuned easily and it could be done by online tuning for better tracking (Tian et al., 2019; Chen et al., 2020; Lee et al., 2020; Li et al., 2020; Ostadian et al., 2020; Sun et al., 2020; Niu et al., 2022). Here, the power of the load was exchanged predominantly to provide steady-state demand of load by using the fuel cell system. Xu et al. (2019) designed a frequency decoupling scheme. It ensured that the SC and batteries provided high-frequency demand, whereas fuel cells provided low-frequency demand through the wavelet, filter, and rapid Fourier transform approaches. The frequency decoupling scheme prevented the stresses on the primary source and improved the lifetime of the proton exchange membrane fuel cell. Constant mean load power was provided by the chief source (Hegazy et al., 2012; El Fadil et al., 2014; Rajabzadeh et al., 2016; Armghan et al., 2018; Li et al., 2019; Demircali et al., 2020; Sai Chandan et al., 2020). In cases where the power of the load was higher or lower than the mean value, SC and batteries will charge and discharge, respectively. Wang et al. (2020) proposed a cost function optimization technique for better operation of the fuel cell to attain maximum global efficiency and fuel economy. The equivalent fuel consumption minimization approach (ECMS) was developed for rapid application. The power exchange was governed by the instantaneous cost function minimization. It consisted of two-way-like consumption of fuel in the overall fuel cell system and equivalent consumption of fuel in SC and battery (Shen et al., 2015; Min et al., 2023).

Real-time PMS for HESS is model predictive control (Njoya Motapon et al., 2014), neural networks, H-infinity, dynamic programming, and adaptive optimal control. These types of PMS are complex and require larger computations. It mainly affects the PMS response time (Hu et al., 2020; Tifour et al., 2020; Yang et al., 2022).
In this paper, the coyote algorithm-based power management scheme for hybrid electric vehicle applications is implemented by utilizing a hybrid energy storage system. It can manage the energy among fuel cells and batteries through the extremely varied state of the load. The performance of PEMFC depends on many operating parameters like temperature, humidity, and pressure, and it also depends on the degree of degradation performance. This paper is systematized as ensues. Section 2 labels the mathematical modeling of HESS. Section 3 represents power management strategies. Section 4 focuses on the comparison of different PMS. Finally, Section 5 presents the conclusion of the research work and scope followed by references.

2 Architecture of the hybrid electric vehicle (HEV) test system

The structure of the hybrid electric vehicle (HEV) test system is seen in Figure 1. The fuel cell, rechargeable battery, and supercapacitor are the three sources of power as shown in this setup. A DC/DC boost converter has been used with the fuel cell to enhance its voltage level toward the desired level and sustain this at the outputs. Supercapacitors have been integrated into bi-directional converters which enable power to be exchanged in both directions. The HESS is concerned with uni-directional as well as bi-directional DC-DC converters for efficient power exchange to allocate HESS energy to load or load to HESS using various power management strategies/schemes (PMS). The optimum fuel economy can be achieved when creating the proper PMS. PMS must be kept to a minimum in hybrid energy sources because it has the potential to shorten their life cycle. Load power is calculated by using Equation (1).

\[
  P_{\text{Load}} = \left( \frac{1}{2} \rho_{\text{air}} SC v^2 + MgC_r + M \frac{dv}{dt} \right) v \tag{1}
\]

2.1 Modeling of battery

The battery is designed with a modest controlled power supply in series with such a fixed resistance. Eq. 2 defines the battery voltage \( V_{\text{bat}} \).

\[
  V_{\text{bat}} = E - R_{\text{bat}} I_{\text{bat}} \tag{2}
\]
The controlled source voltage is calculated by using Eq. 3.

\[
E = E_0 - K \frac{Q}{Q_0} - \int i \, dt + A \exp\left(-B \int i \, dt\right)
\]  

(3)

Where \(E\) represents no load voltage (V), \(E_0\) denotes a constant voltage of the battery (V), \(K\) states the polarization voltage (V), and \(Q\) indicates the capacity of the battery (Ah), whereas \(A\) denotes the amplitude of the exponential zone (V), and \(B\) denotes inverse time constant of the exponential zone (Ah)^{-1}.

FIGURE 8
Waveforms of the Uni-directional DC/DC converter (A) Load current of FC. (B) FC input voltage. (C) FC output voltage. (D) FC Current. (E) The duty cycle of the uni-directional converter.

FIGURE 9
Waveforms of the Bi-directional DC/DC converter (A) Load current of SC. (B) SC input voltage. (C) SC Output voltage. (D) SC current. (E) The duty cycle of the uni-directional converter. (F) The duty cycle of the directional converter.
2.2 Modeling of fuel cell

A fuel cell is a power conversion device that converts chemical energy in hydrogen fuel to electrical power without using heat or mechanical power. As per the chemical process defined in Eq. 4, the basic working principle of a fuel cell is described by a chemical process in which oxygen and hydrogen are linked together to form power, heat, and water.
There are several types of fuel cell technologies that are categorized depending on their electrolytes. Another type of fuel that is widely used in vehicular applications is Proton Exchange Membrane Fuel (PEMFC). There are several new fuel cell prototypes, each with a combination of benefits and drawbacks based on the topic under study. Any model must be concise and accurate. Furthermore, this paper presents a simple electrochemical concept that might be used to determine the behavior of such fuel cells both in dynamic and static conditions. A hydrogen fuel design used in this study was based on the interaction between the fuel cell voltage level and hydrogen, water, and oxygen absolute pressures. The detailed layout of an FC is utilized as a controlled supply voltage. A fuel cell voltage is regulated via oxygen and hydrogen relative pressure, the chemical process temperature of membrane hydration, and the output current. The mathematical model is given as:

\[ V_{FC} = E_{\text{Nernst}} - V_{\text{act}} - V_{\text{ohmic}} - V_{\text{con}} \]  

Where \( E_{\text{Nernst}} \) represents the mean value of the thermodynamic potential in every single cell unit, and it is calculated by Eq. 6 [10].

\[
E_{\text{Nernst}} = 1.229 - 0.85 \times 10^{-3}(T - 298.15) + 4.3085 \times 10^{-3}T[\ln(P_{H_2}) + 0.5 \times \ln(P_{O_2})] 
\]

where,

\[ V_{\text{act}} = \text{Activation voltage drop} \]
\[ V_{\text{ohmic}} = \text{ohmic voltage drop} \]
\[ V_{\text{con}} = \text{Concentration voltage drop} \]

Hence, For \( N \) no. of cells connected in series, the stack voltage \( V_{\text{stack}} \) is described as;

\[ V_{\text{stack}} = NV_{\text{FC}} \]  

The fuel cell's polarization curves indicate the voltage of the battery as a factor of output current. Under several temperatures and hydrogen pressure levels, the following and above results can be seen. Overall polarization patterns for FCs increase as that of the optimal temperature and hydrogen pressure reduce. As much as this is provided by oxygen and fuel to sustain a chemical reaction mechanism, a fuel cell can produce a constant amount of power. Proton exchange membrane fuel cells are widely used in automotive applications due to their high-power density and low and moderate operating temperatures. Furthermore, its effectiveness when reacting under peak load has been restricted because of certain chemical processes which occur in FC. As an outcome, such sources are integrated into the batteries as well as the supercapacitor-based hybrid storage systems.

2.2.1 Fuel cell converter topology (uni-directional)

Normally, DC/DC converters are divided into two categories based on whether or not they utilize galvanic isolation. As an outcome, a non-isolated or isolated circuit might be built. Non-
isolated converters appear to be simple, but to minimize ripple current, a significant input inductor is required. As a response, for protective measures, isolation only between outputs and inputs is often essential. Under this work, an isolated DC/DC converter has two main components: a high-frequency DC-AC converter and an AC-DC converter, which are separated by a transformer to maintain the galvanic isolation between the fuel cell and the load. As a response, high-frequency operations minimize the
converter’s weight and size. The power converter’s design can be seen in Figure 2. It is used to create the electrical connection between both the fuel cell and the DC bus. Through this converter, uni-directional current DC-DC conversion is performed. These converters modify the batteries’ voltage range at the DC link in charging mode.

2.2.2 Control strategy of the uni-directional converter

A converter’s voltage output should be regulated toward the DC bus voltage. As a result, including a proportional-integral controller (PI) to operate the converters is required, as shown in Figure 3.

2.2.3 State space analysis of uni-directional converter

Both the output capacitor voltage and its inductor current were considered state variables to determine the typical design of a DC/DC converter. As selected variables, an FC voltage and its current demand are specified. The equation for state space formulation (8) is as follows:

\[
\begin{cases}
  x = Ax + Bu \\
  y = Cx
\end{cases}
\]  

(8)

Where,

\[
\begin{align*}
  x &= [i_c, V_{DC}]^T \\
  u &= [V_{FC}, \dot{i}_c]^T \\
  y &= V_{DC}
\end{align*}
\]

The given mathematical model describes the state representation of a converter model during period T as such a parameter on duty ratio d:

\[
\frac{di_c}{dt} = \begin{pmatrix}
  \frac{-2R_{eq}}{L_{eq}} - \frac{(1 - 2d)r_{eq}}{L} - \frac{2d}{L} - \frac{(1 - 2d)}{L} & 0 \\
  \frac{2d}{L_{eq}} - 1 & 0
\end{pmatrix} \begin{pmatrix}
  i_c \\
  V_{DC}
\end{pmatrix} + \begin{pmatrix}
  \frac{4md}{L_{eq}} \\
  0
\end{pmatrix} \begin{pmatrix}
  0 \\
  \frac{2d - 1}{C_0} - \frac{2d}{C_{eq}}
\end{pmatrix} \begin{pmatrix}
  v_{fc} \\
  \dot{i}_c
\end{pmatrix} \begin{pmatrix}
  y = [0 1]^T
\end{pmatrix} \begin{pmatrix}
  i_c \\
  V_{DC}
\end{pmatrix}
\]  

(9)

Where,

\[
\begin{align*}
  R_{eq} &= 2r_d + 2m^2r_T \\
  L_{eq} &= L + m^2L_T \\
  C_{eq} &= C_0 + \frac{C_e}{m^2}
\end{align*}
\]

(10)

2.3 Modeling of supercapacitors

Supercapacitors are one of the recent advancements for power storage devices, especially integrated devices. A capacitance $C_{SC}$ is linked to an equivalent series resistance $R_{SC}$ under this setup. The below formula is used to determine a supercapacitor voltage $V_{SC}$ as a result of SC current $I_{SC}$:

\[
V_{SC} = V_1 - R_{SC} \times I_{SC} = \frac{Q_{SC}}{C_{SC}} - R_{SC} \times I_{SC}
\]  

(11)

Where, $Q_{SC}$ denotes the quantity of electricity present in the cell, and the power of the supercapacitor is calculated by using Eq. 12,

\[
P_{SC} = \frac{Q_{SC}}{C_{SC}} \times I_{SC} - R_{SC} \times I_{SC}^2
\]  

(12)

Utilizing supercapacitors like a storage system in such an electric vehicle implies the construction of such stacking of cells, where $N_S$ cells are interconnected in series and $N_P$ cells are parallel connected. Eqs 13, 14 determine the capacity and resistance of the supercapacitor stack.

\[
C_{SC} = C_{dom} \frac{N_P}{N_S}
\]  

(13)

\[
R_{SC} = R_{ndom} \frac{N_S}{N_P}
\]  

(14)

Eqs 15, 16 determine both the current and voltage of a stack as a measure of such component current and voltage.

\[
V_{SC} = N_P \times V_{elem}
\]  

(15)

\[
I_{SC} = N_P \times I_{elem}
\]  

(16)

2.3.1 Supercapacitor converter topology (bi-directional)

Both batteries and supercapacitors are employed to store energy in the transportation system under investigation. Two-way current converters are designed to transfer power both ways and are required to connect these two parts toward the DC link.

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### TABLE 1 Overall performance of each PMS scheme.

<table>
<thead>
<tr>
<th>Drive cycle</th>
<th>Criteria for PMS</th>
<th>PI</th>
<th>SMC</th>
<th>FDFC</th>
<th>ECMS</th>
<th>EEMS</th>
<th>COA</th>
</tr>
</thead>
<tbody>
<tr>
<td>WLTC (Worldwide Harmonized Light Vehicle Test Cycles)</td>
<td>State of charge of the battery (%)</td>
<td>70-52</td>
<td>70-54</td>
<td>70.53</td>
<td>70-53</td>
<td>70-59</td>
<td>70-59</td>
</tr>
<tr>
<td></td>
<td>Consumption of H₂ (g)</td>
<td>31.5</td>
<td>30.83</td>
<td>33.29</td>
<td>38.13</td>
<td>33.19</td>
<td>22.74</td>
</tr>
<tr>
<td></td>
<td>Overall efficiency (%)</td>
<td>76.16</td>
<td>77.28</td>
<td>71.83</td>
<td>72.11</td>
<td>78.19</td>
<td>81.29</td>
</tr>
<tr>
<td></td>
<td>Stress on battery (σ)</td>
<td>28</td>
<td>24.81</td>
<td>27.9</td>
<td>29.4</td>
<td>24.46</td>
<td>24.38</td>
</tr>
<tr>
<td></td>
<td>Stress on fuel cell (σ)</td>
<td>24.23</td>
<td>23.19</td>
<td>21.84</td>
<td>27.17</td>
<td>19.23</td>
<td>19.82</td>
</tr>
<tr>
<td></td>
<td>Stress on Ultracapacitor (σ)</td>
<td>36.12</td>
<td>32.45</td>
<td>31.93</td>
<td>34.92</td>
<td>37.1</td>
<td>31.15</td>
</tr>
</tbody>
</table>
Some of these converters are assembled by using various components.

- Four transistor-diode pairs are comprised of a full bridge ultracapacitor.
- The four-transistor-diode set full bridge end DC bus has been used.
- With the use of winding inductance, two different planar transformers supply galvanic isolation as well as power storage.

Because all these converters linked by SC and also battery were comparable, then the focus was on the one that was related to capacitors in this study. Figure 4 depicts the topologies used in this study.

### 2.3.2 Control strategy of the Bi-directional converter

Two proportional integral controllers are used to regulate the two converters (DC/AC) and (AC/DC). As a result, as indicated in Figure 5, its converter’s output voltage can be controlled toward the DC link voltage.

### 2.3.3 State space analysis of Bi-directional converter

Multiple system parameters, namely, converter output voltage and inductor current, were considered as model parameters for modeling the converters connected with capacitors, and even the supercapacitor voltage or current required was preferred as dependent variables, relating to a situation of a fuel cell.

A) Boost mode operation (Ultra-capacitor Discharging)

The set of calculations in Eq. 17 represents the state characterization of the converters model when it is working in boost mode.

\[
\begin{align*}
\dot{x} &= A_1 x + B_1 u \\
y &= C_1 x
\end{align*}
\]  
(17)

The matrices \(A_1\), \(B_1\), and \(C_1\) are calculated using Eqs 18, 19

\[
A_1 = \begin{pmatrix} 0 & 4(d - 1) \\ 1 - d & \frac{m(L - L_r)}{mC_{eq}} \end{pmatrix}
\]  
(18)

\[
B_1 = \begin{pmatrix} \frac{2(d - 0.5)}{L} & \frac{8(1 - d)}{L + L_r} & \frac{2(d - 1)}{C_{eq}} & \frac{2(d - 0.5)}{C_0} \\ 0 & 0 & 0 & 0 \end{pmatrix}
\]  
(19)

\[
C_1 = \begin{pmatrix} 0 & 1 \end{pmatrix}
\]  
(20)

with:

\[
\begin{align*}
L_{eq} &= mL(L + L_r) \\
C_{eq} &= C_0 + \frac{C_r}{m}
\end{align*}
\]  
(21)

B) Buck mode operation (Ultra-capacitor charging)

In this case, Eq. 22 denotes the state classification of the converter layout under buck mode.

\[
\begin{align*}
\dot{x} &= A_2 x + B_2 u \\
y &= C_2 x
\end{align*}
\]  
(22)

\[
A_2 = \begin{pmatrix} 0 & -4d \\ d & \frac{m(L + L_r)}{mC_{eq}} \end{pmatrix}
\]  
(23)

\[
B_2 = \begin{pmatrix} (1 - d) & 8d & 0 \\ \frac{L}{L} & \frac{L + L_r}{2d} & \frac{2(d - 1)}{C_{eq}} \\ 0 & 0 & \frac{C_r}{C_0} \end{pmatrix}
\]  
(24)

\[
C_2 = \begin{pmatrix} 0 & 1 \end{pmatrix}
\]  
(25)

### 2.4 Problem formulation

In the FCHEV, managing the power between HESS(FC/B/SC) enhances the better performance of the hybrid storage system. The traditional EEMS employs \(f_{\text{min}}\) as a function from a Matlab toolbox. Consequently, for enhancing the performance, the \(f_{\text{min}}\) function is replaced by a recent optimization algorithm called the coyote optimization algorithm (COA). In the process of optimization, the input and output variables are fuel cell output power \(P_{\text{FC}}\), battery state of charge \(\text{SOC}\), and power \(P_{\text{batt, SOC}}\). The upper limits and lower limits are given as \(P_{\text{FC, min}} = 580W, P_{\text{FC, max}} = 8800W, P_{\text{batt, min}} = 1500W, P_{\text{batt, max}} = 3400W\), \(\text{SOC, min} = 60, \text{SOC, max} = 90\).

In this EEMS technique, hydrogen consumption \((H2)\) is minimized by raising the battery and SC demand. EEMS technique requires the battery and SC cost function; it does not require the determined battery energy calculation. From Figure 4, it is shown that the EEMS algorithm inputs are DC bus voltage and state of charge of the battery or supercapacitor and the outputs are charge/discharge voltage \((\Delta V)\) supercapacitor and battery reference power. Hence, comparing the battery and load power, the FC’s reference power via FC current \((I_{\text{FC}})\) is derived. The SC charge/discharge voltage is obtained by estimating the actual voltage of the DC bus with the sum of the DC bus reference voltage \((V_{\text{Volt}})\) and SC’s voltage. In this process of the EEMS optimization problem, the SC charge/discharge voltage \((\Delta V)\) and power of the battery \((P_{\text{batt}})\) have to be assessed. The minimized objective function is power supplied via SC and battery during a definite time interval and is described as follows.

Minimize: \(J = - \left( P_{\text{batt}} \Delta T + \frac{1}{2} C_r \Delta V^2 \right) \)  
(26)

In the EEMS optimization process, based on the power produced by the battery, the objective function is subjected to inequality constraints and the constraints are subject to \(P_{\text{batt}} \Delta T \leq (\text{SOC} - \text{SOC, min}) \cdot V_{\text{batt}} \cdot Q\)  
(27)

Whereas the power of the battery and voltage of the DC bus parametric inequality constraints are formulated as follows:

\[
P_{\text{batt, min}} \leq P_{\text{batt}} \leq P_{\text{batt, max}}
\]  
(28)

\[
V_{\text{DC, min}} \leq V_{\text{DC}} \leq V_{\text{DC, max}}
\]  
(29)
Here, $P_{\text{batt}} \Delta T$ denotes the delivered battery power over a sampling time ($\Delta T$). $C_{r}$ represents the rated capacitance of SC. $V_{\text{DCmin}}$ and $V_{\text{DCmax}}$ denote the minimum and maximum limit of DC bus voltage. $V_{\text{batt}}$ represents the battery’s nominal voltage. $Q$ denotes the battery-rated capacity.

From Eq. 26, for maximizing the objective function, the proposed COA uses a COA optimizer by considering the constraints in Eq. 27. The configuration of the COA algorithm is shown in Figure 5. The inputs of COA are the state of charge of the battery and voltage of the supercapacitor, while the outputs of COA are supercapacitor charge/discharge voltage and reference power of the battery, in which these are compared with the supercapacitor voltage and load.

The PI controller supplies the required current to the battery converter and the conflicts between the voltage of the supercapacitor and reference are adjusted by this controller. Here, the contrast between the power of the battery and demand is subjected to the fuel cell reference current.

### 3 Description of proposed coyote algorithm

In 2018, Perez et al proposed a coyote optimization algorithm (COA). This is a metaheuristic type of algorithm; the idea was inspired by the species called *Canis latrans* species which lives in North America. In the optimization process, the COA algorithm can manage a balance between the exploitation phase and the exploration phase. COA mainly depends on acting the coyotes, and it experiences the coyotes’ interchanging performance. Figures 6, 7 shows block diagram and birth and death rules of Coyote optimization algorithm. Coyotes can identify a prey location and they also have a strong sense of smell.

In COA, the initiation of the population is split into no. of packs (NP) with no. of coyotes (NC). In a Pth pack, the optimization process starts to calculate each coyote in Pth pack is calculated as follows:

$$\text{SOC}_{C_i}^{t+1} = h_{ij} + r_{ij}(u_{h_{ij}} - l_{h_{ij}})$$ (30)

Here, the designed variables of upper and lower limits are ($u_{h_{ij}}$) and ($l_{h_{ij}}$). $r_{ij}$ represents the range of random numbers [0,1]. In the present social condition, the coyotes are adapted by the representation of fitness function, and it is expressed as follows:

$$f_{it}^{l_{ij}} = f_{it}^{p_{t}}(\text{SOC}_{C_i}^{t+1})$$ (31)

At the beginning of the optimization process, the coyotes are randomly allocated to packs. In some cases, coyotes leave their packs or join another pack; this act can arise with a probability of

$$P_e = 0.005N_{C_i}^{l_{ij}}$$ (32)

### 4 Results and discussion

#### 4.1 Waveforms of the uni-directional converter

The various waveforms of the uni-directional converter, which is designed for fuel cells, are presented in Figure 8. Figure 8A shows the change in load current waveform. Figures 8B, D show the effect of load current fluctuation on fuel cell voltages and currents. Due to the use of the PI controller, the converter output voltage [shown in Figure 8C] remains stable even when a large load current is desired. As a result, as seen in Figure 8E, the duty ratio is based on the load current.

#### 4.2 Waveforms of the Bi-directional converter

The simulation results of a supercapacitor connected to a DC/DC buck-boost converter in terms of improving the reliability and efficiency and how the load current often affects the supercapacitor are shown in Figure 9. Figure 9 depicts the simulation outcomes. As a result, the supercapacitor current and voltage are shown in Figures 9B, C for the load current shown in Figures 9A, D. Because the load current has both positive and negative levels, the supercapacitor is either charging or discharging depending on the current direction, as shown by the state of the charge waveform in Figure 9E. Despite current variations, the output voltage is kept stable and identical to the set point, allowing the PI regulator’s performance to be confirmed. Figure 9F depicts its duty cycle. It fluctuates in response to changes in current in terms of managing the converter and keeping the output voltage even at the base value.

#### 4.3 Hydrogen consumption, overall efficiency, and stress analysis

Different power management approaches for hybrid storage architectures were implemented. Each power management system was implemented with the same initial conditions: the state of charge of the battery was 70%, the temperature of the battery was 30°C, the voltage of the supercapacitor was 270 V, the temperature of the supercapacitor was 25°C, the voltage of the fuel cell was 52 V, and the temperature of the fuel cell was 40°C. The FC/B/SC model included a 12.5 kW, 30–60 V PEMFC, a 48 V, 40 Ah Li-ion battery, and a pair of 15.6 F, 291.6 V-6 series-connected supercapacitors. Two DC/DC converters managed the battery storage. The converter discharged the battery in a 4 KW boost mode and charged the battery in a 1.2 KW buck mode. A comparison of alternative power management systems is based on hydrogen consumption, overall efficiency, fuel cell and battery stress. Figures 10, 11 show the consumption of hydrogen (in lpm and grams), and Figure 12 shows the total efficiency of all power management strategies. The stress evaluation for fuel cell, battery, and supercapacitor energy was done at 270 V DC using the Haar wavelet technique. Haar wavelet decomposition was used to assess power deterioration in low- and high-frequency equipment. The component with the highest frequency has a zero-mean value, and the standard deviation ($\sigma$) of this module offers more information on how a distinct storage system is maintained. The quantity of hydrogen consumed (in grams) is stated as:

$$\text{Cons}_{H_2} = \frac{N}{F} \int_{0}^{1000} i_{H_2} \, dt$$ (33)
Here, F = Faraday fundamental (A.s/mol). Global efficiency is represented as,

\[ \eta_{\text{Efficiency}} = \frac{P_{\text{load}}}{P_{\text{FC}} + P_{\text{batter}} + P_{\text{cap}}} \]

(34)

Here, \( P_{\text{FC}} \), \( P_{\text{batter}} \), \( P_{\text{cap}} \) = Power of FC/B/UC

4.4 SoC of battery and supercapacitor voltage

The battery is quickly discharged while the primary source-fuel cell controls the load and charges to reach the SoC reference in the traditional PI technique. In the case of state machine control, the fuel cell charges supercapacitors beyond their reference voltage (270 V) when the SoC of the Li-ion battery bank reaches its minimal limit, requiring the DC bus to regulate in order to charge the batteries. As opposed to other strategies, the frequency decoupling fuzzy logic strategy uses fuel cells to supply constant power, allowing the battery to recharge. Higher battery power is employed, which improves the performance of an equivalent consumption minimization strategy and an external energy minimization technique. In Figures 13, 14, the fluctuation of the battery SOC voltage and current is depicted.

Since the Li-ion battery and UC are almost at the same level of charge, it follows that they will both be completely charged when the primary input is turned off. The battery and UC currents can now be raised. As a result, the interface voltages of the UC and batteries decrease as they are used to satisfy the rising load need. The load is changed at the same time that the battery and UC conditions are altered.

This indicates that the power produced by the battery bank and the UC bank is superior to the power supplied by the FC for delivering the necessary load, resulting in the lowest hydrogen usage.

4.5 Distribution of power to load

As seen in Figure 15, the electricity for the load was provided by hybrid energy sources (FC, B, and UC), and the overall comparison of EMS schemes is shown in Table 1. The system’s performance was measured over a period of 350 s, starting at time zero, when there was no demand for the load and no-load power. In this instance, the fuel cell charged the battery. The power supply to batteries and supercapacitors was distributed during the 1940s, while fuel cell power steadily increased at the same time. At 45 s later, the voltage level in the supercapacitor dropped to the reference value of 270 V. At time \( t = 60 \) s, the supercapacitor was supplying more transient demand than the primary source’s maximum power, while the power of the fuel cell was increasing primarily. Therefore, additional fuel cell power was used to charge the secondary sources. As a result of the decreasing load requirement at 330 s, the power of the primary source likewise gradually decreased when recharging the battery container.

5 Conclusion

In order to manage the energy in the hybrid-producing system made up of fuel cells, batteries, and supercapacitors as efficiently as possible, this work proposes a contemporary optimization technique known as COA. To supply the rapidly fluctuating demand, the hybrid system is connected to a DC-DC converter. As a backup emergency supply, the hybrid-producing system/hybrid energy storage system is being provided for optimization. By optimizing the energy supplied by both the batteries and the supercapacitors, the primary goal is to decrease overall hydrogen consumption. The COA is used by the authors because of its simplicity and need for a few control settings, among other benefits. The suggested COA’s outcomes are contrasted with those of other traditional and heuristic methods, including state machine control strategy, rule-based fuzzy logic strategy, classical proportional integral control strategy, equivalent consumption reduction strategy, and genetic algorithm. The comparison focuses on how much hydrogen is consumed and how effective the plan is. With just 30.28 g of hydrogen used and a 78.02% efficiency, the suggested method is discovered to be superior to the other alternatives. The outcomes of the suggested COA’s analysis support the approach’s validity and superior in terms of achieving the best possible energy management for the hybrid generating system. The findings showed that the suggested COA may greatly reduce energy consumption when high-frequency operation of transportation vehicles, such as high-speed trains and aircraft, is used. Applying another cutting-edge optimization method will allow this work to be expanded upon and refined in the future. The overall cost of operating the system and the voltage control of each source are two additional objective functions that may be considered.

Data availability statement

The original contributions presented in the study are included in the article/Supplementary material, further inquiries can be directed to the corresponding author.

Author contributions

Conceptualization, VM and YO; supervision, YO; validation, VM; visualization, VM; writing–original draft, VM and YO; writing–review and editing, VM and YO. All authors contributed to the article and approved the submitted version.

Conflict of interest

The authors declare that the research was conducted in the absence of any commercial or financial relationships that could be construed as a potential conflict of interest.
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References


